An Activity Completion Duration based Checkpoint Selection Strategy for Dynamic Verification of Fixed-time Constraints in Grid Workflow Systems

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Abstract: In grid workflow systems, to verify fixed-time constraints efficiently at the run-time execution stage, some checkpoints are often selected so that we only need to conduct the fixed-time constraint verification at such checkpoints rather than at all activity points. However, the existing typical checkpoint selection strategies are inefficient and/or ineffective because they may incur some unnecessary verification by selecting some unnecessary checkpoints or omit some necessary verification by omitting some necessary checkpoints. Therefore, in this paper, based on the run-time activity completion duration, we develop a new checkpoint selection strategy that is more efficient and effective than the existing typical checkpoint selection strategies. The final comparison and quantitative evaluation further demonstrate this point.

1 Introduction

Grid workflow systems, which are evoking a high degree of interest aim to support modelling, redesign and execution of large-scale sophisticated e-science and e-business processes using the grid computing approach to enable the coordinated use of numerous distributed and heterogeneous resources [Ab04, Ca03, Cy04, Fo02]. In Open Grid Services Architecture (OGSA), a grid workflow can be defined as the automation of a Grid process, in whole or part, during which documents, information or data are passed from one grid service to another for action, according to a set of procedural rules [Am04, Cy04, CY05, Hu03]. Conceptually, a grid workflow is a collection of activities, and the dependencies between activities that define their execution orders and form four basic control structures: sequential, parallel, selective and iterative [Cy04]. These activities are implemented and executed by corresponding grid services. The whole working process of a grid workflow system can be divided into three stages: build-time, run-time instantiation and run-time execution. At the build-time stage, grid workflow specifications are defined by deploying some grid workflow definition languages such as
Grid Services Flow Language (GSFL), Abstract Grid Workflow Language (AGWL), Service Workflow Language (SWFL) and Grid Workflow Execution Language (GWEL) [Cy04, FPV04, Hu03, KWL02]. At the run-time instantiation stage, grid workflow instances are created, and especially grid services specified in the build-time definition documents are discovered by an instantiation service that is a high-level grid service [Cy04, KWL02]. At the run-time execution stage, the grid workflow instances are executed, and the execution is coordinated between grid services by the grid workflow engine that itself is a high-level grid service, hence automatically grid aware [Cy04, Hu03, KWL02].

To control the temporal correctness of the grid workflow specification and execution, fixed-time constraints are often set [CY04, EPR99, MO99]. A fixed-time constraint at an activity is an absolute time value by which the activity must be completed. For example, a climate modelling grid workflow must be finished by the scheduled time [Ab04], say 9:00pm, so that the weather forecasting can be broadcasted at a later time, say 10:30pm, on the same day. Here, 9pm is a fixed-time constraint.

After the fixed-time constraints are set, the temporal verification is conducted to check whether they are all consistent. At the build-time and run-time instantiation stages, the temporal verification is static because of no any specific execution times. For each fixed-time constraint, we conduct its verification once only with the consideration of all covered activities. Therefore, we need not decide at which activities we should conduct the fixed-time constraint verification. At the run-time execution stage, the activity completion duration is uncertain, which may affect the consistency of a fixed-time constraint. Hence, we may need to verify a fixed-time constraint many times at different activities. However, conducting the verification at every activity is not efficient because we may not have to do so at some activities such as those activities which can be completed within the allowed time interval. Therefore, a question is prompted which is: “where should we conduct the fixed-time constraint verification?”. The activities at which we conduct the fixed-time constraint verification are called checkpoints [CYC04, De03, MO99, ZCP01]. Correspondingly, a research field comes into the picture whose topic is checkpoint selection strategies [CYC04, De03, MO99, ZCP01].

So far, some typical checkpoint selection strategies have been proposed. [De03] takes every activity as a checkpoint. We denote this strategy as CSS1 (CSS: Checkpoint Selection Strategy). [ZCP01] sets checkpoints at the start time and end time of each activity and each flow. We denote this strategy as CSS2. [MO99] takes the start point of a workflow instance as a checkpoint and adds a checkpoint after each decision activity is executed. We denote this strategy as CSS3. [MO99] also mentions another checkpoint selection strategy: user-defined checkpoints. We denote this strategy as CSS4. [CYC04], as our previous work, proposes a checkpoint selection strategy based on the run-time activity completion duration. We denote this strategy as CSS5. However, since the activity completion duration is uncertain, we may not have to conduct the fixed-time constraint verification at some activities. Therefore, CSS1 and CSS2 are inefficient. Similarly, CSS3 and CSS4 are inefficient either as we may not have to conduct the fixed-time constraint verification at the start activity or the decision activities or the user-defined activities. In addition, CSS5 and CSS6 are ineffective because we will omit the
verification which should be conducted at some other activities. As to CSS\textsubscript{2}, in [CYC04], a fixed-time constraint only has two states: CC (Conventional Consistency) and CI (Conventional Inconsistency) and CSS\textsubscript{1} is based on it. However, according to the analysis in [CY05\textsubscript{b}], in the grid workflow systems, a fixed-time constraint should have four states: SC (Strong Consistency), WC (Weak Consistency), WI (Weak Inconsistency) and SI (Strong Inconsistency). CC corresponds to SC and CI is divided into WC, WI and SI. Based on CSS\textsubscript{2}, we can judge whether we should take an activity as a checkpoint for CC or CI verification. However, since CSS\textsubscript{1} is only based on CC and CI, we are not able to further consider whether we should take the activity as a checkpoint for the verification of WC, WI or SI. As a result, the corresponding verification is omitted. Hence, CSS\textsubscript{1} is ineffective either.

Regarding the above limitations of the existing typical checkpoint selection strategies, in this paper, we develop a new checkpoint selection strategy. The strategy is based on the relationship between the run-time activity completion duration and the four states: SC, WC, WI and SI, and can select the checkpoints dynamically along the grid workflow execution. The final comparison and quantitative evaluation further show that our strategy is more efficient and effective than the existing typical ones.

The remainder of the paper is organised as follows. Section 2 describes a timed grid workflow representation. Section 3 details our checkpoint selection strategy. Section 4 further shows the benefits of our strategy through a comparison and quantitative evaluation. Section 5 concludes our contributions and points out the future work.

2 Timed Grid Workflow Representation

Based on the directed graph concept, a grid workflow can be represented by a grid workflow graph, where nodes correspond to activities and edges correspond to dependencies between activities, called flows [CM00, EPR99]. Here we assume that the grid workflow is well structured. As far as the time is concerned, an activity is similar to a flow. Therefore, we use term “activity” to refer to the real activity as well as the flow. Based on [CY04, CY05\textsubscript{a}, EPR99, MO99], we denote the \textit{i}\textsuperscript{th} activity of a grid workflow as \textit{a\textsubscript{i}}, the expected time from which the specification of the grid workflow \textit{g}\textsubscript{w} will become effective as \textit{C\textsubscript{ie}(g\textsubscript{w})}. For each \textit{a\textsubscript{i}}, we denote its maximum duration, minimum duration, average duration, run-time start time, run-time end time and run-time completion duration as \textit{D(a\textsubscript{i})}, \textit{d(a\textsubscript{i})}, \textit{Ave(a\textsubscript{i})}, \textit{S(a\textsubscript{i})}, \textit{E(a\textsubscript{i})} and \textit{Rcd(a\textsubscript{i})} respectively. \textit{Rcd(a\textsubscript{j})} covers the queuing delay, synchronisation delay, network latency and so on caused at \textit{a\textsubscript{j}}. If there is a fixed-time constraint at \textit{a\textsubscript{i}}, we denote it as \textit{FTC(a\textsubscript{i})} and its value as \textit{Fv(a\textsubscript{i})}. If there is a path from \textit{a\textsubscript{i}} to \textit{a\textsubscript{j}} (\textit{j\geq i}), we denote the maximum duration, minimum duration, average duration, run-time real completion duration between them as \textit{D(a\textsubscript{i}, a\textsubscript{j})}, \textit{d(a\textsubscript{i}, a\textsubscript{j})}, \textit{Ave(a\textsubscript{i}, a\textsubscript{j})} and \textit{Rcd(a\textsubscript{i}, a\textsubscript{j})} respectively [EPR99, MO99]. Normally we have \textit{d(a\textsubscript{i}) \leq Ave(a\textsubscript{i}) \leq D(a\textsubscript{i})} and \textit{d(a\textsubscript{i}, a\textsubscript{j}) \leq Ave(a\textsubscript{i}, a\textsubscript{j}) \leq D(a\textsubscript{i}, a\textsubscript{j})}. For convenience, we consider one execution path in the grid workflow without losing generality. As to a selective or parallel structure, for each branch, it is an execution path. For an iterative structure, from the start time to the end time, it is still an execution path. Therefore, for the selective/parallel/iterative structure, we can also apply the results achieved from one
execution path. Hence, from $a_t$ to $a_p$, $D(a_t, a_p)$, $d(a_t, a_p)$ and $Ave(a_t, a_p)$ is equal to the sum of activity maximum durations, minimum durations and average durations respectively.

Besides the above time attributes, in [CY05b], we have defined the four consistency states: SC, WC, WI and SI. Because we will develop a new checkpoint selection strategy based on them, we should present a summary of their definitions. In addition, for the comparison between CSS, and our strategy in Section 4, we also need to summarise the definitions of CC and CI. However, since the checkpoint concept is related to the run-time execution stage, we only summarise the definitions of the stage below. The definitions of other stages and detailed discussion can be referred to [CY04, CY05b].

**Definition 1.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of SC when $Rcd(a_t, a_t) + D(a_t, a_t) \leq frv(a_t) - S(a_t)$.

**Definition 2.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of WC when $Rcd(a_t, a_t) + Ave(a_t, a_t) \leq frv(a_t) - S(a_t) < Rcd(a_t, a_t) + D(a_t, a_t)$.

**Definition 3.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of WI when $Rcd(a_t, a_t) + d(a_t, a_t) \leq frv(a_t) - S(a_t) < Rcd(a_t, a_t) + Ave(a_t, a_t)$.

**Definition 4.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of SI when $frv(a_t) - S(a_t) < Rcd(a_t, a_t) + D(a_t, a_t)$.

**Definition 5.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of CC when $Rcd(a_t, a_t) + D(a_t, a_t) \leq frv(a_t) - S(a_t)$.

**Definition 6.** At the run-time execution stage, at checkpoint $a_t$ which is either before or at $a_t$, $FTC(a_t)$ is said to be of CI when $frv(a_t) - S(a_t) < Rcd(a_t, a_t) + D(a_t, a_t)$.

For clarity, we further depict SC, WC, WI, SI, CC and CI in Figure 1.

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**Figure 1:** Definitions of SC, WC, WI and SI vs definitions of CC and CI at run-time execution stage

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3 A New Checkpoint Selection Strategy

According to [CY05b, HA00], WI and SI will be adjusted to SC or WC by the corresponding exception handling. Therefore, along the grid workflow execution, at an activity point, before the execution of the activity, all fixed-time constraints will be of either SC or WC. However, after the execution of the activity, the uncertain activity completion duration may affect their consistency. Therefore, we now firstly discuss the relationship between the activity completion duration and SC, WC, WI & SI. Then, we present our checkpoint selection strategy based on the relationship.

3.1 Relationship between Activity Completion Duration and SC, WC, WI & SI

At the run-time execution stage, at activity point a_p it's completion duration is Rcd(a_p). We discuss its relationship with SC, WC, WI and SI by deriving some theorems that will form the basis for presenting our checkpoint selection strategy.

**Theorem 1.** At activity point a_p, if D(a_p) < Rcd(a_p), 1) all previous WC fixed-time constraints cannot be of SC and 2) may be of WC, WI or SI; and 3) previous SC fixed-time constraints may be of SC, WC, WI or SI.

**Proof:** 1) Suppose FTC(a_u) is of WC before the execution of a_p (p≤m), according to Definition 2, we have: fvt(a_u)-S(a_j) < Rcd(a_j, a_p, t) + D(a_p, a_u). If D(a_p) < Rcd(a_p), then, we have: fvt(a_u)-S(a_j) < Rcd(a_j, a_p, t) + D(a_p, a_u) + D(a_p, a_u) = Rcd(a_j, a_p, t) + D(a_p, a_u). Hence, we have:

\[
\text{fvt}(a_u)-S(a_j) < \text{Rcd}(a_j, a_p, t) + \text{D}(a_p, a_u)
\]

However, for FTC(a_u) to be of SC, we must ensure (2) below holds.

\[
\text{Rcd}(a_j, a_p, t) + \text{D}(a_p, a_u) \leq \text{fvt}(a_u)-S(a_j)
\]

Obviously, (2) does not hold. Hence, FTC(a_u) cannot be of SC after a_p's execution.

2) From D(a_p) < Rcd(a_p), we have: Rcd(a_j, a_p, t) + Ave(a_p, a_u) = Rcd(a_j, a_p, t) + Ave(a_p) + Ave(a_p) ≥ Rcd(a_j, a_p, t) + Ave(a_p) + Ave(a_p) ≥ Rcd(a_j, a_p, t) + Ave(a_p) + Ave(a_p). Hence, we have:

\[
\text{Rcd}(a_j, a_p, t) + \text{Ave}(a_p, a_u) < \text{Rcd}(a_j, a_p, t) + \text{Ave}(a_p, a_u)
\]

Meanwhile, because FTC(a_u) is previously of WC, we have:

\[
\text{Rcd}(a_j, a_p, t) + \text{Ave}(a_p, a_u) \leq \text{fvt}(a_u)-S(a_j)
\]

However, from (2) and (4), we can not judge whether (5) below holds.

\[
\text{Rcd}(a_j, a_p, t) + \text{Ave}(a_p, a_u) \leq \text{fvt}(a_u)-S(a_j)
\]

If (5) holds, FTC(a_u) is of WC again. However, depending on specific Rcd(a_p), (5) may or may not hold. Similarly, we may or may not have Rcd(a_j, a_p, t) + d(a_p, a_u) ≤ fvt(a_u)-S(a_j) < Rcd(a_j, a_p, t) + Ave(a_p, a_u), and we also may or may not have fvt(a_u)-S(a_j) < Rcd(a_j, a_p, t) + Ave(a_p, a_u). Therefore, according to Definitions 2, 3 and 4, depending on specific Rcd(a_p), FTC(a_u) may be of WC, WI or SI.

3) Suppose FTC(a_u) is of SC before the execution of a_p (p≤n), according to Definition 1, we have:
\[
Rcd(a_i, a_{p-1}) + D(a_p, a_n) \leq \text{ftv}(a_p) - S(a_i)
\]  
(6)

From \(D(a_p) < Rcd(a_{p-1})\), we have: \(Rcd(a_i, a_{p-1}) + D(a_p, a_n) = Rcd(a_i, a_{p-1}) + D(a_p, a_n)\) \(< Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) = Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p)\). Hence, we have:

\[
Rcd(a_i, a_{p-1}) + D(a_p, a_n) < Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p)
\]  
(7)

However, from (6) and (7), we can not judge whether (8) below holds.

\[
Rcd(a_i, a_{p-1}) + D(a_{p+1}, a_n) \leq \text{ftv}(a_{p+1}) - S(a_i)
\]  
(8)

If (8) holds, \(FTC(a_{p-1})\) is of SC again. However, depending on specific \(Rcd(a_{p-1})\), (8) may or may not hold. Similarly, we may or may not have \(Rcd(a_i, a_{p-1}) + \text{Ave}(a_{p-1}, a_p) \leq \text{ftv}(a_{p-1}) - S(a_i)\). If \(Rcd(a_p) < D(a_{p-1})\), then we have: \(Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) = Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p)\). Hence, we have:

\[
Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) \leq \text{ftv}(a_{p-1}) - S(a_i)
\]  
(9)

According to Definition 1, \(FTC(a_i)\) is still of SC after the execution of \(a_p\).

2) The proof is similar to 3) of Theorem 1 and consequently is omitted.

In overall terms, the theorem holds.

**Theorem 2.** At activity point \(a_p\), if \(Rcd(a_p) \leq D(a_p)\), 1) all previous SC fixed-time constraints are still of SC; and 2) previous WC fixed-time constraints may be of SC, WC, WI or SI.

**Proof:** 1) Suppose \(FTC(a_i)\) is of SC before the execution of \(a_p\) \((p \leq n)\), according to Definition 1, we have \(Rcd(a_i, a_{p-1}) + D(a_p, a_n) \leq \text{ftv}(a_p) - S(a_i)\). If \(Rcd(a_p) \leq D(a_{p-1})\), then we have: \(Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) = Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p)\). Hence, we have:

\[
Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) \leq \text{ftv}(a_{p-1}) - S(a_i)
\]  
(9)

According to Definition 1, \(FTC(a_i)\) is still of SC after the execution of \(a_p\).

2) The proof is similar to 3) of Theorem 1 and consequently is omitted.

In overall terms, the theorem holds.

**Theorem 3.** At activity point \(a_p\), if \(Rcd(a_p) \leq \text{Ave}(a_p)\), 1) all previous SC fixed-time constraints are still of SC; and 2) all previous WC fixed-time constraints are of either WC or SC; and 3) if they are still of WC, the status has been changed for better.

**Proof:** 1) The proof is similar to 1) of Theorem 2 and consequently is omitted.

2) Suppose \(FTC(a_p)\) is of WC before the execution of \(a_p\) \((p \leq m)\), according to Definition 2, we have:

\[
Rcd(a_i, a_{p-1}) + \text{Ave}(a_p, a_n) \leq \text{ftv}(a_p) - S(a_i) = Rcd(a_i, a_{p-1}) + D(a_p, a_n)
\]  
(10)

If \(Rcd(a_p) \leq \text{Ave}(a_p)\), then we have: \(Rcd(a_i, a_{p-1}) + \text{Ave}(a_p, a_n) = Rcd(a_i, a_{p-1}) + \text{Ave}(a_p, a_n)\). Hence, we have:

\[
Rcd(a_i, a_{p-1}) + \text{Ave}(a_p, a_n) \leq \text{ftv}(a_p) - S(a_i)
\]  
(11)

In addition, we also have: \(Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) = Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p)\). Hence, we have:

\[
Rcd(a_i, a_{p-1}) + D(a_{p-1}, a_p) \leq \text{ftv}(a_{p-1}) - S(a_i)
\]  
(11)
\[ Rcd(a_p, a_{p+1}) + D(a_{p+1}) \leq Rcd(a_p, a_{p+1}) + D(a_p + a_{p+1}) \]  

However, from (8), (9), and (10) that we only have, we cannot judge whether (9) or (10) holds.

\[ ftv(a_{p+1}) - S(a_i) < Rcd(a_p, a_{p+1}) + D(a_{p+1}) \]  

\[ Rcd(a_p, a_{p+1}) + D(a_{p+1}) \leq ftv(a_{p+1}) - S(a_i) \]

In fact, depending on how much \( Rcd(a_p) \) is less than \( Ave(a_p) \), (9) or (10) may or may not hold. If (9) holds, then, with (10), we have:

\[ Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \leq ftv(a_{p+1}) - S(a_i) < Rcd(a_p, a_{p+1}) + D(a_{p+1}) \]

According to Definition 2, (9) means that \( FTC(a_n) \) is of WC. If (10) holds, according to Definition 1, \( FTC(a_n) \) is already switched to be of SC after the execution of \( a_p \).

3) If \( Rcd(a_p) \leq Ave(a_p) \), then we have:

\[ Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \leq Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \]

\[ Ave(a_p, a_{p+1}) \leq Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \]

Therefore, we have:

\[ Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \leq Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n) \]

Correspondingly, we have:

\[ [ftv(a_{p+1}) - S(a_i)] - [Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n)] \leq [ftv(a_{p+1}) - S(a_i)] - [Rcd(a_p, a_{p+1}) + Ave(a_{p+1}, a_n)] \]

(7) means that, after the execution of \( a_p \), \( FTC(a_n) \) is closer to SC than before. Therefore, the status of \( FTC(a_n) \) has been changed for better.

In overall terms, the theorem holds.

Based on Theorems 1, 2 and 3, we can derive the detailed relationship between the completion duration of \( a_p \) and SC, WC, WI & SI. For clarity, we depict it in Figure 2.

![Figure 2: Relationship between completion duration of \( a_p \) and SC, WC, WI & SI](image)

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3.2 Checkpoint Selection

According to the discussion in Section 3.1, we can draw the following conclusions:

- If \( D(a_p) < Rcd(a_p) \), we have to verify all previous SC and WC fixed-time constraints. However, for previous WC fixed-time constraints, we need not verify whether they are of SC.

- If \( Rcd(a_p) \leq D(a_p) \), we need not verify all previous SC fixed-time constraints. But we have to verify all previous WC fixed-time constraints.

- If \( Rcd(a_p) \leq Ave(a_p) \), we need not verify all previous SC fixed-time constraints. As to previous WC fixed-time constraints, we borrow some conclusions from [CY05b] and we need not verify them either. In [CY05b], we already developed a method to adjust the WC fixed-time constraints to be of SC. According to Theorem 3, after the execution of \( a_p \), the status of the previous WC fixed-time constraints is changed for better (even can be changed to SC). Therefore, we can still use the previous adjustment. Hence, we need not verify it.

Based on the above conclusions, we can decide whether or not we should take \( a_p \) as a checkpoint and correspondingly we derive a new checkpoint selection strategy. For convenience of the discussion, we denote it as \( CSS_{ACD} \) (Activity Completion Duration based Checkpoint Selection Strategy).

\( CSS_{ACD} \) is: At activity \( a_p \), if \( D(a_p) < Rcd(a_p) \), we take it as a checkpoint for the verification of SC, WC, WI & SI of all previous SC fixed-time constraints, and for the verification of WC, WI & SI of all previous WC fixed-time constraints. If \( Rcd(a_p) \leq D(a_p) \), we take \( a_p \) as a checkpoint for the verification of SC, WC, WI & SI of all previous WC fixed-time constraints. If \( Rcd(a_p) \leq Ave(a_p) \), we do not take \( a_p \) as a checkpoint.

According to \( CSS_{ACD} \), we can further derive Algorithm 1 that combines the checkpoint selection process of \( CSS_{ACD} \) and the fixed-time constraint verification. Algorithm 1 is depicted on next page due to the space limit of this page.

By applying Algorithm 1, we can base the fixed-time constraint verification on \( CSS_{ACD} \). As a result, we only need to conduct the fixed-time constraint verification at necessary activity points. And at such points, we only need to verify those fixed-time constraints that we should verify.
symbol Definitions:
ArraySC: an array of all previous SC fixed-time constraints that cover \( a_i \);
ArrayWC: an array of all previous WC fixed-time constraints that cover \( a_i \).
end Definitions
Input: ArraySC, ArrayWC, \( S(a_i) \), \( Rcd(a_i) \), \( Ave(a_i) \), maximum, minimum and average durations of all activities involved in ArraySC and ArrayWC;
Output: checkpoint report and SC, WC, WI & SI report;
If \( D(a_j) < Rcd(a_i) \) then
Output ‘\( a_j \) is a checkpoint for the verification of SC, WC, WI and SI of all previous SC fixed-time constraints, and for the verification of WC, WI and SI of all previous WC fixed-time constraints’
while (not end of ArraySC) do
// verify SC, WC, WI and SI of previous SC fixed-time constraints
Select current fixed-time constraint from ArraySC, say \( FTC(a_i) \) (\( p \leq j \));
if \( (Rcd(a_i), a_j) + D(a_{j-1}, a_i) \leq brv(a_i)-S(a_i) \) then
Output ‘FTC\( (a_i) \) is of SC’;
else if \( (Rcd(a_i), a_j) + Ave(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + D(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WC’;
else if \( (Rcd(a_i), a_j) + d(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + Ave(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WI’;
else if \( (brv(a_i)-S(a_i) < Rcd(a_i, a_j)+d(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of SI’;
end if
end while
while (not end of ArrayWC) do // verify WC, WI and SI of previous WC fixed-time constraints
Select current fixed-time constraint from ArrayWC, say \( FTC(a_i) \) (\( p \leq j \));
if \( (Rcd(a_i), a_j) + Ave(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + D(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WC’;
else if \( (Rcd(a_i), a_j) + d(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + Ave(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WI’;
else if \( (brv(a_i)-S(a_i) < Rcd(a_i, a_j)+d(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of SI’;
end if
end while
end if
end while
else if \( Ave(a_j) < Rcd(a_i) \leq D(a_j) \) then
Output ‘\( a_j \) is a checkpoint for the verification of SC, WC, WI and SI of all previous WC fixed-time constraints’;
while (not end of ArrayWC) do // verify SC, WC, WI and SI of previous WC fixed-time constraints
Select current fixed-time constraint from ArrayWC, say \( FTC(a_i) \) (\( p \leq j \));
if \( (Rcd(a_i), a_j) + D(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) \) then
Output ‘FTC\( (a_i) \) is of SC’;
else if \( (Rcd(a_i), a_j) + Ave(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + D(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WC’;
else if \( (Rcd(a_i), a_j) + d(a_{j-1}, a_j) \leq brv(a_i)-S(a_i) < Rcd(a_i, a_j) + Ave(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of WI’;
else if \( (brv(a_i)-S(a_i) < Rcd(a_i, a_j)+d(a_{j-1}, a_j) \) then
Output ‘FTC\( (a_i) \) is of SI’;
end if
end while
end if
else
Output ‘\( a_j \) is NOT a checkpoint and there is no need of any fixed-time constraint verification’;
end if

Algorithm 1: Checkpoint selection and fixed-time constraint verification based on CSS\( _{ACD} \)
4 Comparison and Quantitative Evaluation

In this section, we will evaluate our checkpoint selection strategy CSS_{CD} by comparing it with other strategies: CSS_{D}, CSS_{I}, CSS_{I}, CSS_{I}, CSS_{D}, CSS_{D}, and CSS_{I}, which are stated in Section 1. Since CSS is similar to CSS as they both set checkpoints at every activity. And CSS is similar to CSS as they both define the checkpoints before the grid workflow execution. Therefore, we only analyse CSS, CSS, CSS, and CSS_{CD}.

According to the discussion in Section 3, to compare CSS, CSS, CSS, and CSS_{CD}, we should analyse the unnecessary and omitted fixed-time constraint verification based on them respectively. According to the definitions of the fixed-time constraint consistency in Section 2, the primary fixed-time constraint verification computation is focused on the sum of the maximum durations between two activities. Therefore, we take each computation of the maximum duration addition as a verification computation unit. Correspondingly, we analyse CSS, CSS, CSS, and CSS_{CD} by comparing their unnecessary and omitted verification computation unit numbers. We denote the unnecessary and omitted verification computation unit numbers of CSS as une_{uc}, and omi_{ou}, respectively, CSS as une_{uc}, and omi_{ou}, respectively, CSS as une_{uc}, and omi_{ou}, respectively, CSS_{CD} as une_{uc}_{inc}, and omi_{ou}_{inc}, respectively.

We consider a climate modelling grid workflow that may consist of hundreds and thousands of activities and must be time constrained so that the weather forecasting can be broadcasted on time [Abb04]. For simplicity, we focus on one fixed-time constraint in it, say FTC(A). We suppose FTC(A) covers N activities. Since in the real-world grid workflow systems, normally there are many grid workflow instances, we conduct the quantitative analysis in a statistical way. Therefore, we introduce possibility Q for an activity execution not exceeding its average duration (0\leq Q\leq 1). For simplicity, we assume that each activity has the same Q. We now conduct the corresponding comparison between CSS, and CSS_{CD} in Section 4.1, and between CSS, and CSS_{CD} in Section 4.2, and between CSS, and CSS_{CD} in Section 4.3. The comparison between CSS, CSS, and CSS_{I} is beyond the scope of this paper as we are focusing on the development and discussion of CSS_{CD}.

4.1 CSS_{CD} vs CSS

According to the consistency definitions in Section 2 and the discussion of CSS_{CD} in Section 3, we can derive the following computing equations:

\[
\begin{align*}
\text{une}_{uc} &= Q*N, \\
\text{omi}_{ou} &= 0, \\
\text{une}_{ec}_{ou} &= 0, \\
\text{omi}_{ou}_{inc} &= 0
\end{align*}
\]

Suppose \(N = 20\), with \(Q\) changing, we list corresponding une_{uc}, omi_{ou}, une_{ec}_{ou}, and omi_{ou}_{inc} in Table 1. The value selection of \(N\) does not affect our analysis because what we want is the trend of how une_{uc}, omi_{ou}, une_{ec}_{ou}, and omi_{ou}_{inc} are changing with \(Q\) changing.

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Table 1: Comparison of unnecessary and omitted verification between CSS\textsubscript{CD} and CSS\textsubscript{I}

<table>
<thead>
<tr>
<th>( Q )</th>
<th>0.0</th>
<th>0.1</th>
<th>0.2</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.8</th>
<th>0.9</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{une}_{CSS\textsubscript{CD}} )</td>
<td>0</td>
<td>40</td>
<td>80</td>
<td>120</td>
<td>160</td>
<td>200</td>
<td>240</td>
<td>280</td>
<td>320</td>
<td>360</td>
<td>400</td>
</tr>
<tr>
<td>( \text{une}_{CSS\textsubscript{I}} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \text{omi}_{CSS\textsubscript{CD}} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \text{omi}_{CSS\textsubscript{I}} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

From the above computing equations and Table 1, we can see the following facts:

* \( \text{omi}_{CSS\textsubscript{CD}} \) and \( \text{omi}_{CSS\textsubscript{I}} \) are always 0. In fact, based on CSS\textsubscript{I}, we conduct the fixed-time constraint verification at every activity. Therefore, there is no omitted verification. Based on CSS\textsubscript{CD}, we conduct the verification only at any activity whose completion duration is more than its average duration. According to Section 3, we should do so. Therefore, there is no omitted verification either. Therefore \( \text{omi}_{CSS\textsubscript{CD}} = \text{omi}_{CSS\textsubscript{I}} = 0 \).

* \( \text{une}_{CSS\textsubscript{CD}} \) is always 0. \( \text{une}_{CSS\textsubscript{I}} \) is also 0 if \( Q=0 \). In fact, based on CSS\textsubscript{CD}, we conduct the verification at any activity whose completion duration is more than its average duration. And according to Section 3, we should do so. Therefore, \( \text{une}_{CSS\textsubscript{CD}} \) is always 0. Based on CSS\textsubscript{I}, we conduct the verification at every activity. If \( Q=0 \), the execution of every activity will exceed its average duration. According to Section 3, we should conduct the verification at every activity. Therefore, all verification based on CSS\textsubscript{I} becomes necessary. Hence, \( \text{une}_{CSS\textsubscript{I}} = 0 \).

* With \( Q \) increasing, \( \text{une}_{CSS\textsubscript{CD}} \) is increasing. This means that the more activities that can be completed with their average durations, the more amount of unnecessary verification based on CSS\textsubscript{I}. However, the amount of the unnecessary verification based on CSS\textsubscript{CD} does not change and is always less than that based on CSS\textsubscript{I}.

In summary, although CSS\textsubscript{I} does not omit any fixed-time constraint verification, it may cause some unnecessary verification. Especially, the more activities that can be completed within their average durations, the more amount of the unnecessary verification based on CSS\textsubscript{I}. The unnecessary verification will eventually affect the overall verification efficiency. Hence, CSS\textsubscript{CD} is more efficient than CSS\textsubscript{I}.

### 4.2 CSS\textsubscript{CD} vs CSS\textsubscript{I}

We suppose there are \( M \) checkpoints defined by CSS\textsubscript{I}. Then, according to the definitions in Section 2, we can derive the following computing equations for CSS\textsubscript{I}:

\[
\text{une}_{CSS\textsubscript{I}} = Q \cdot M \cdot N \quad \text{omi}_{CSS\textsubscript{I}} = (1-Q) \cdot (N-M) \cdot N
\]

We now take some specific values to see how they perform. Suppose \( N = 20 \) and \( M = 3 \). The selection of the values does not affect our analysis because what we want is the...
trend of how $u_{e,c_{e}}$ and $o_{m,c_{e}}$ are changing with $Q$ changing. With $Q$ changing, we list corresponding $u_{e,c_{e}}$ and $o_{m,c_{e}}$ in Table 2. For clarity, we also list corresponding $u_{e,c_{e,cd}}$ and $o_{m,c_{e,cd}}$ in Table 2 although they have been listed in Table 1.

Table 2: Comparison of unnecessary and omitted verification between $CSS_{ACD}$ and $CSS_{e}$

<table>
<thead>
<tr>
<th>$Q$</th>
<th>0.0</th>
<th>0.1</th>
<th>0.2</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.8</th>
<th>0.9</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u_{e,c_{e}}$</td>
<td>0</td>
<td>6</td>
<td>12</td>
<td>18</td>
<td>24</td>
<td>30</td>
<td>36</td>
<td>42</td>
<td>48</td>
<td>54</td>
<td>60</td>
</tr>
<tr>
<td>$u_{e,c_{e,cd}}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$o_{m,c_{e}}$</td>
<td>340</td>
<td>306</td>
<td>272</td>
<td>238</td>
<td>204</td>
<td>170</td>
<td>136</td>
<td>102</td>
<td>68</td>
<td>34</td>
<td>0</td>
</tr>
<tr>
<td>$o_{m,c_{e,cd}}$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

From the above computing equations and Table 2, we can see the following facts:

• As discussed in Section 4.1, $u_{e,c_{e,cd}}$ and $o_{m,c_{e,cd}}$ are always 0.

• If $Q=0$, $u_{e,c_{e}}=0$. In fact, based on $CSS_{e}$, we conduct the verification at $M$ predefined activities. If $Q=0$, the execution of every activity will exceed its average duration. Then, according to the discussion in Section 3, we must conduct the verification at every activity. Hence, all verification at $M$ prescribed activities becomes necessary and consequently $u_{e,c_{e}}=0$.

• With $Q$ increasing, $u_{e,c_{e}}$ is increasing. This means that the more activities that can be completed within their respective average durations, the more amount of the unnecessary verification based on $CSS_{e}$.

• If $Q=1$, $o_{m,c_{e}}=0$. In fact, if $Q=1$, all activities can be completed within their average activities, according to Section 3, we need not conduct any verification. Namely, we will not omit any verification by $CSS_{e}$. Hence, $o_{m,c_{e}}=0$. This is the best case for $o_{m,c_{e}}$.

• With $Q$ decreasing, $o_{m,c_{e}}$ is increasing. This means that the more activities at which we should conduct the verification, the more omitted verification based on $CSS_{e}$.

In summary, on one hand, $CSS_{e}$ may cause some unnecessary fixed-time constraint verification. The more activities that can be completed within their respective average durations, the more amount of the unnecessary verification based on $CSS_{e}$. However, $CSS_{ACD}$ does not incur any unnecessary verification. Since the unnecessary verification will eventually affect the overall verification efficiency, $CSS_{ACD}$ is more efficient than $CSS_{e}$. On the other hand, $CSS_{e}$ may omit some necessary verification. The more activities where we should conduct the fixed-time constraint verification, the more omitted verification will be incurred. However, $CSS_{ACD}$ does not omit necessary verification.
Since the omitted verification will eventually affect the overall verification effectiveness, \( CSS_{ACD} \) is more effective than \( CSS_i \).

### 4.3 \( CSS_{ACD} \) vs \( CSS_i \)

According to the discussion in Section 3 and [CYC04], at \( a_i \), if \( D(a_i) < Rcd(a_i) \), then both \( CSS_{ACD} \) and \( CSS_i \) take \( a_i \) as a checkpoint. Therefore, for the situation where \( D(a_i) < Rcd(a_i) \), \( CSS_{ACD} \) and \( CSS_i \) are the same in terms of the unnecessary and omitted verification computation. Hence, we need not consider the situation and for simplicity, we can assume that the possibility for the situation be 0. Then, we derive the following computing equations.

\[
\text{une}_{c_{st}} = 0 \quad \text{omi}_{c_{st}} = (1 - Q) \times N^2
\]

We now take some specific values to see how they perform. We suppose \( N = 20 \). The value selection of \( N \) does not affect our analysis because what we want is the trend of how \( \text{une}_{c_{st}} \) and \( \text{omi}_{c_{st}} \) are changing with \( Q \) changing. With \( Q \) changing, we list corresponding \( \text{une}_{c_{st}} \) and \( \text{omi}_{c_{st}} \) in Table 3. For clarity, we also list corresponding \( \text{une}_{c_{st},e} \) and \( \text{omi}_{c_{st},e} \) in Table 3 although they have been listed in Tables 1 and 2.

<table>
<thead>
<tr>
<th>( Q )</th>
<th>0.0</th>
<th>0.1</th>
<th>0.2</th>
<th>0.3</th>
<th>0.4</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.8</th>
<th>0.9</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{une}<em>{c</em>{st}} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \text{une}<em>{c</em>{st},e} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>( \text{omi}<em>{c</em>{st}} )</td>
<td>400</td>
<td>360</td>
<td>320</td>
<td>280</td>
<td>240</td>
<td>200</td>
<td>160</td>
<td>120</td>
<td>80</td>
<td>40</td>
<td>0</td>
</tr>
<tr>
<td>( \text{omi}<em>{c</em>{st},e} )</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

From the above computing equations and Table 3, we can see the following facts:

- As discussed in Section 4.1, \( \text{une}_{c_{st},e} \) and \( \text{omi}_{c_{st},e} \) are always 0.

- \( \text{une}_{c_{st}} \) is always 0. In fact, according to \( CSS_{ACD} \), we only conduct the fixed-time constraint verification at any activity whose completion duration is more than its maximum duration. And according to the discussion in Section 3, at an activity, if its completion duration is more than its average duration, we should conduct the verification. According to Section 2, the activity average duration is not more than the maximum duration. Hence, all verification based on \( CSS_i \) is necessary. Hence \( \text{une}_{c_{st}} = 0 \).

- If \( Q = 1 \), \( \text{omi}_{c_{st}} = 0 \). In fact, if \( Q = 1 \), all activities can be completed within their respective average durations, according to Section 3, we need not conduct any verification. Namely, we will not omit any verification by \( CSS_i \). Hence, \( \text{omi}_{c_{st}} = 0 \).
• With \( Q \) decreasing, \( \text{omi}_\text{avg} \) is increasing. This means that the more activities whose completion durations are more than their respective average durations and less than or equal to their respective maximum ones, the more omitted verification based on \( \text{CSS}_J \).

In summary, \( \text{CSS}_J \) may omit some necessary fixed-time constraint verification. The more activities whose completion durations are more than their respective average durations and less than or equal to their respective maximum durations, the more necessary verification will be omitted. However, \( \text{CSS}_{ACD} \) does not omit necessary verification. Since the omitted fixed-time constraint verification will eventually affect the overall verification effectiveness, \( \text{CSS}_{ACD} \) is more effective than \( \text{CSS}_J \).

5 Conclusions and Future Work

In this paper, based on the analysis of the limitations of the existing typical checkpoint selection strategies, and the analysis of the relationship between the run-time activity completion duration and SC (Strong Consistency), WC (Weak Consistency), WI (Weak Inconsistency) and SI (Strong Inconsistency), a new checkpoint selection strategy named \( \text{CSS}_{ACD} \) has been developed. \( \text{CSS}_{ACD} \) selects the checkpoints dynamically along the grid workflow execution. The final comparison and quantitative evaluation have shown that, compared to the existing typical checkpoint selection strategies, our strategy \( \text{CSS}_{ACD} \) is more efficient and effective. With these contributions, we can further investigate some problems such as temporal exception handling when a fixed-time constraint is violated at a checkpoint, and the mechanisms by which we can predict future possible checkpoints.

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References


